

Combining Functions

① Performing operations with function
 $\hookrightarrow +, -, \times, \div$

To combine two functions, $f(x)$ and $g(x)$

Sum of functions

$$h(x) = f(x) + g(x)$$

$$h(x) = (f+g)(x)$$

\uparrow first combining the functions
 first + then evaluate w/
 the given x value.

Difference of functions

$$h(x) = f(x) - g(x)$$

$$h(x) = (f-g)(x)$$

The combined function $h(x) = (f \cdot g)(x)$ represent
the product of two functions $f(x) \cdot g(x)$

$$f(x) \cdot g(x) = (f \cdot g)(x)$$

The combined function $h(x) = \left(\frac{f}{g}\right)x$ where it represents the quotient of two functions $f(x)$ and $g(x)$

$$\frac{f(x)}{g(x)}$$

x cannot be equal to 0.
 $g(x) \neq 0.$

The domain of a product or quotient of function is the domain that is common to both $f(x)$ and $g(x)$

$$\begin{array}{ll} f(x) & D: (-\infty, \infty) \\ g(x) & D: [0, \infty) \end{array} \quad] \quad \begin{array}{l} \text{The } \underline{\text{common}} \\ \text{domain is} \\ [0, \infty) \end{array}$$

CH 3 pg 22 on example booklet

Pg 22 b) inverse of the function. Sketch the $f(x)$ and $f^{-1}(x)$

$$y = (x - 2)^2 + 5 \quad \leftarrow \text{Quadratic function written in vertex form}$$

The vertex is $(2, 5)$
The lead coefficient is +1 which means parabola opens up.

Determine the inverse function of $f(x)$.

$$y = (x - 2)^2 + 5$$
$$x = (y - 2)^2 + 5 \quad \begin{array}{l} \text{switch places of } x \text{ and } y \\ \text{variables.} \end{array}$$
$$\sqrt{x-5} = \sqrt{(y-2)^2}$$
$$\pm \sqrt{x-5} = y - 2 \quad \begin{array}{l} \text{solve for } y \text{ (meaning} \\ \text{isolate } y \text{ on one side of} \\ \text{equation. Do this} \\ \text{algebraically.)} \end{array}$$
$$2 \pm \sqrt{x-5} = y$$

$$y = 2 \pm \sqrt{x-5}$$

Graphing

